

☐ Data from 10mm gauge block of EIM_DIM_01 in nm

$$l_1 := 0 \quad l_2 := 10 \quad l_3 := 10 \quad l_4 := 20 \quad l_5 := 10 \quad u_x := 14.9$$

v evaluated as usual: $v_a := \max(l_1, l_2, l_3, l_4, l_5) - \min(l_1, l_2, l_3, l_4, l_5)$



Evaluation with infinite degrees of freedom

$$N := 20000$$

$$D1 := \text{rnorm}(N, l_1, u_x) \quad D2 := \text{rnorm}(N, l_2, u_x) \quad D3 := \text{rnorm}(N, l_3, u_x)$$

$$D4 := \text{rnorm}(N, l_4, u_x) \quad D5 := \text{rnorm}(N, l_5, u_x)$$

$$D := \text{augment}(D1, D2, D3, D4, D5)$$

$$V := \text{for } i \in 0..N-1$$

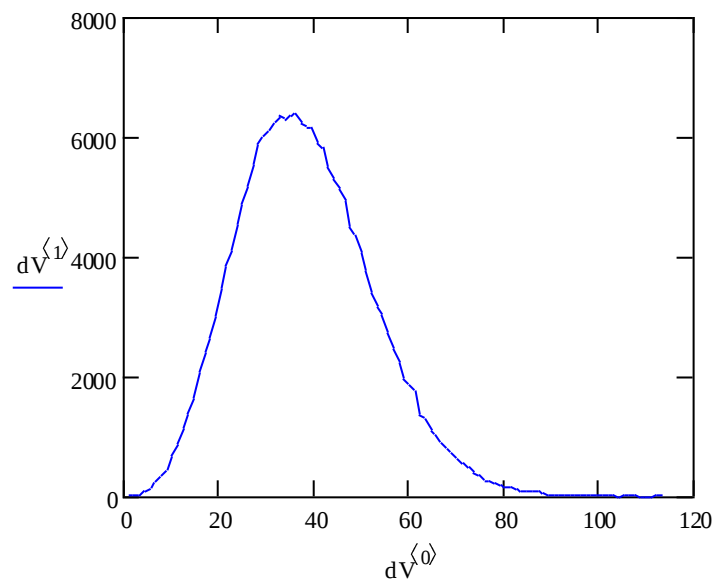
$$w_i \leftarrow \max(D_{i,0}, D_{i,1}, D_{i,2}, D_{i,3}, D_{i,4}) - \min(D_{i,0}, D_{i,1}, D_{i,2}, D_{i,3}, D_{i,4})$$

$$u_x := \text{stdev}(V)$$

confidence interval calculation: $s_{10000} = 17.147 \quad s_{190000} = 63.25$

$$dV := \text{histogram}(100, V)$$

$$\text{mean}(V) = 38.445 \quad u_x = 14.083$$





Evaluation with finite degrees of freedom

$v := 3$

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v :=
| n ← 200
| m ← 1000
|  $U \leftarrow \sqrt{\frac{u_X^2}{v} \cdot \text{rchisq} \mid n, v}$ 
| for j ∈ 0..n - 1
|   | d1 ← rnorm(m, l1, Uj)
|   | d2 ← rnorm(m, l2, Uj)
|   | d3 ← rnorm(m, l3, Uj)
|   | d4 ← rnorm(m, l4, Uj)
|   | d5 ← rnorm(m, l5, Uj)
|   | d ← augment(d1, d2, d3, d4, d5)
|   | for i ∈ 0..m - 1
|   |   |  $z_{i,j} \leftarrow \max \{ d_{i,0}, d_{i,1}, d_{i,2}, d_{i,3}, d_{i,4} \} - \min \{ d_{i,0}, d_{i,1}, d_{i,2}, d_{i,3}, d_{i,4} \}$ 
|   |   |  $w_j \leftarrow \text{Var} \left( z^{\langle j \rangle} \right)$ 
|   |  $v_{\text{eff}} \leftarrow \frac{2 \cdot u_X^4}{\text{Var}(w)}$ 
|   | y ← z⟨0⟩
|   | for k ∈ 1..n - 1
|   |   | y ← stack(y, z⟨k⟩)
|   |  $\begin{pmatrix} v_{\text{eff}} \\ y \end{pmatrix}$ 

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eff. degrees of freedom: $\nu_0 = 5.635$

confidence interval calculation: $\underline{s} := \text{sort}(\underline{v}_1)$ $s_{10000} = 14.283$ $s_{190000} = 67.597$

$dv := \text{histogram}(dV^{\langle 0 \rangle}, \underline{v}_1)$

